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OF WEAK INTERACTIONS

IN e'e COLLISIONS

Новосибирск

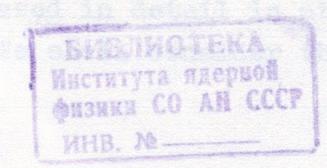
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TESTS OF RENORMALIZABLE MODELS OF WEAK INTERACTIONS IN e⁺e⁻ COLLISIONS

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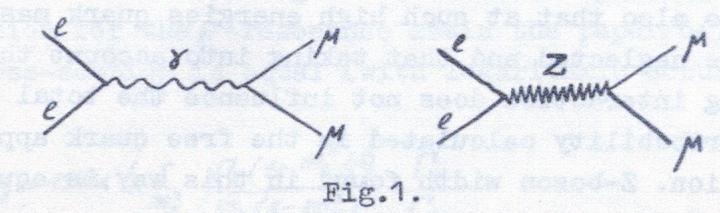
In the frames of Weinberg and Georgi-Glashow models the cross-sections of the processes e[†]e⁻/^{*}/
(in particular near the Z-resonance), e[†]e⁻-Z^{*}/, e[†]e⁻W[†]W⁻, e[†]e⁻-e[†]e^{*}W[†]W⁻ are calculated. The cross-sections of the two last reactions become equal already at the energy 2E = 14m_W.



1. Processes with neutral vector boson

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In the Weinberg model the reaction ete-ptpin the second order in a is described by the two
diagrams given at the fig.1. Simple calculations le-



ad to the following expression for the cross-section of the process

of the process
$$\frac{d\sigma}{ds} = \frac{d^{2}}{4S} \left[1 + \frac{(4\sin^{2}\eta - 1)^{2}}{2\sin^{2}2\eta} \frac{s}{(s - m_{z}^{2})} + \frac{((4\sin^{2}\eta - 1)^{2} + 1)^{2}}{16\sin^{4}2\eta} \frac{s^{2}}{(s - m_{z}^{2})^{2}} \right] \times (1 + \cos^{2}\theta) + \frac{1}{\sin^{2}2\eta} \frac{s}{(s - m_{z}^{2})} \left[1 + \frac{(4\sin^{2}\eta - 1)^{2}}{2\sin^{2}2\eta} \frac{s}{(s - m_{z}^{2})} \right] \cos\theta$$

Here $s = 4E^2$ is the square of the total energy in c.m.s., θ is the angle between the M^- and e^- momenta, m_Z is the Z-boson mass, η is the mixing angle characteristic for the Weinberg model.

The distinctions of this cross-section from the electromagnetic one, charge asymmetry including, are discussed in detail in other works/3,4/.

We shall consider the behaviour of this cross-

section at s~mZ only. Find at first the Z-boson and into hadrons. To estimate the probability of Zboson decays into hadrons we use the model of weak interaction of hadrons based on SU(4) symmetry/5/. Assume also that at such high energies quark masses may be neglected and that taking into account the strong interaction does not influence the total decay probability calculated in the free quark approximation. Z-boson width found in this way is equal

 $\Gamma_{Z}^{2} = \frac{dm_{Z}}{3} \left\{ c dg^{2} \eta + \left[2 + (1 - 2\alpha)^{2} \right] t g^{2} \eta \right\}$ (2)

where Q is the p-quark charge.

In the resonance the total cross-section of the process e'e-M'M looks as follows

$$\sigma_{zes} = \frac{3\pi}{16m_z^2} \left\{ \frac{(1 - 2\sin^2\eta)^2 + 4\sin^4\eta}{\cos^4\eta + [2 + (1 - 2Q)^2]\sin^4\eta} \right\}^2$$
 (3)

The numerical values of $\Gamma_{\rm Z}$ and $\sigma_{\rm res}$ at $\sin^2\eta = 0.3$ and Q = 2/3 are $\Gamma_Z = 0.6$ GeV, $\sigma_{res} = 2 \times 10^{-32}$ cm². Note that the cross-section of elastic ete scattering has in the resonance the same value (if one neglects the Rutherford growth at small angles); the cross-sections of annihilation into hadrons and into $V_{e}\widetilde{V}_{e}$, $V_{\mu}\widetilde{V}_{\mu}$ in the resonance are of the same order. The cross-section of the process ete-ptp decreases rapidly away of the resonance. Therefore, when the total energy is higher than the resonance one, the reaction with photon emission (e e ZZ-8 pt m) which returns the process back to the resonance, becomes more advantageous. (the corresponding calculation for the P-resonance seein the paper/6/). Its cross-section is equal (with logarithmic accuracy) to

$$\sigma_8 = 12\pi i d \ln \frac{S}{m_e^2} \frac{\Gamma_e \left(1 + \frac{m_z^2/S^2}{S^2}\right)}{m_z \left(s - m_z^2\right)} \frac{\Gamma_\mu}{\Gamma_z}$$
Here $\Gamma = \Gamma' = \alpha m_z \frac{(4sin^2\eta - 1)^2 + 1}{s^2}$ are the widths of

 $G_{s} = 12\pi i d \ln \frac{S}{m_{e}^{2}} \frac{\Gamma_{e} \left(1 + \frac{m_{2}^{2}/S}{S}\right)}{m_{2} \left(s - m_{2}^{2}\right)} \frac{\Gamma_{p}}{\Gamma_{z}}$ Here $\Gamma_{e} = \Gamma_{p} = \frac{\alpha m_{z}}{12} \frac{(4sin^{2}p - 1)^{2}+1}{sin^{2}p^{2}}$ are the widths of the decay channels $Z \rightarrow e^{+}e^{-}$ and $Z \rightarrow p^{+}p^{-}$. Formula (4) is valid when $\frac{(s - m_{2}^{2})}{m_{2}\Gamma_{z}^{2}} >> 1$. The process $e^{+}e^{-} = 2p^{+}p^{-}$ dominates over e e + p + m when √s - m ≥1.4 GeV.

Present also for completeness the cross-section of the process Ye-Ze

$$\sigma(8e-Ze) = 6\pi d \ln \frac{(s-m_z^2)^2}{sm_e^2} \frac{\Gamma_e}{m_z s} \left[1 - 2\frac{m_z^2}{s} + 2\frac{m_z^4}{s^2}\right]$$
 (5)

2. W-pair production

Consider now the process ete-W'W. In the Weinberg model this reaction is described by three diagrams (see fig.2). We do not take into account

the interaction with neutral scalar field since it leads to terms proportional to the electron mass.

After averaging over leptons polarizations and summing over those of W-bosons the total cross-section of the process is equal to

$$\sigma = \frac{\pi \chi^{2} \sqrt{\frac{1}{2} \sin^{2} \eta}}{\frac{2 \sin^{2} \eta}{5}} \left\{ \left(1 + \frac{2}{\chi} + \frac{2}{\chi^{2}}\right) \frac{L}{V} - \frac{5}{4} + \frac{m_{2}^{2} (1 - 2 \sin^{2} \eta)}{5 - m_{2}^{2}} \left[\frac{2}{\chi^{2}} (1 + 2 \chi)\right] \frac{L}{V} - \frac{\chi}{12} - \frac{5}{3} - \frac{1}{\chi} + \frac{m_{2}^{4} (8 \sin^{4} \eta - 4 \sin^{2} \eta + 1) \sqrt{\frac{2}{3}}}{48 (s - m_{2}^{2})} \left(\chi^{2} + 20 \chi + 12\right) \right\}$$

Here $x = s/m^2$, m is the W-boson mass, $v = \sqrt{1 - 4/x}$ is its velocity in c.m.s., $L = \ln \frac{1+\sqrt{1-x}}{1-\sqrt{1-x}}$.

At the threshold $(s-4m^2)$

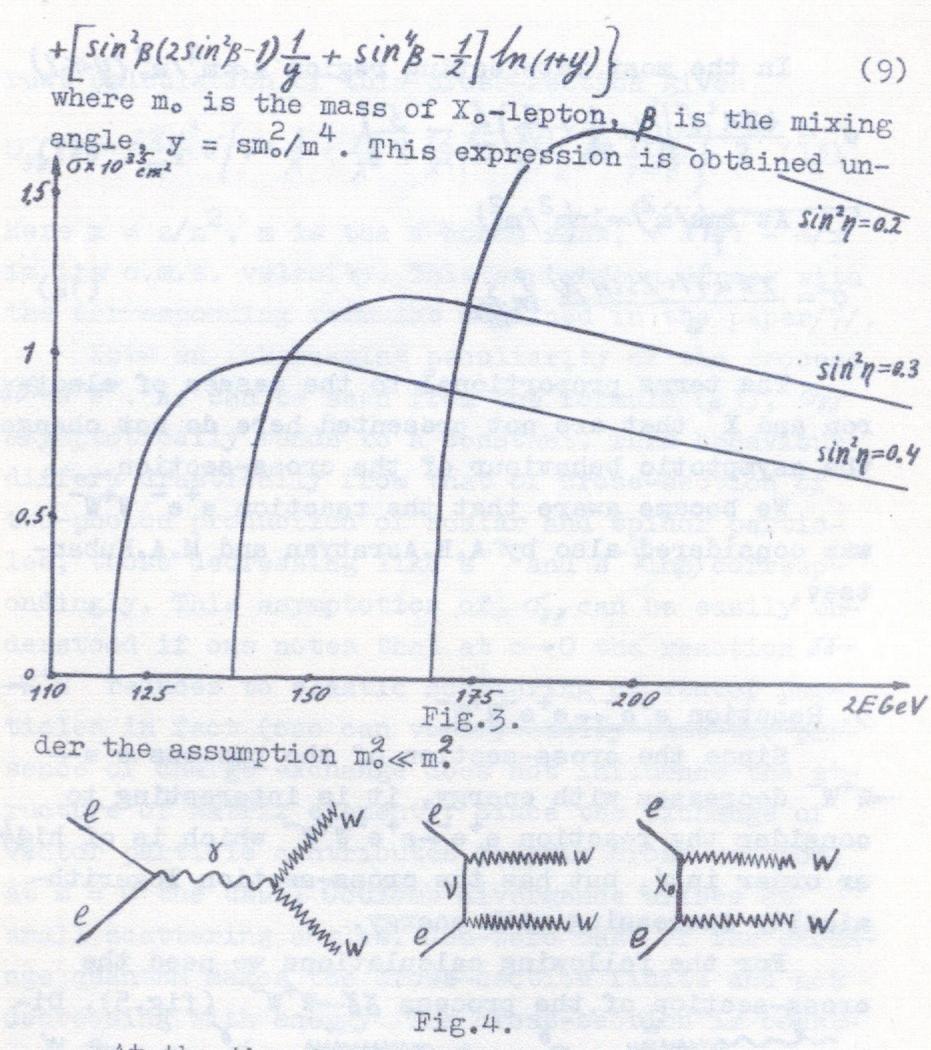
$$\sigma = \frac{\alpha G}{2\sqrt{2}} \frac{V}{\sin^2 \eta} \approx 1.1 \times 10^{-35} \frac{V}{\cos^2 \frac{V}{\sin^2 \eta}}$$
 (7)

Present also for completeness the asymptotic behaviour of the cross-section at s--- $(h\frac{S}{m^2}>>1)$

$$\sigma = \frac{\pi a^2}{2\sin^4 \eta} \int \ln \frac{s}{m^2}$$
 (8)

The energy dependence of the cross-section for various values of the mixing angle are given at the fig.3.

In the Georgi-Glashow model the process $e^+e^ \rightarrow$ W⁺W⁻ is described by the graphs presented at the fig.4. Here the cross-section is equal to $\sigma = \frac{4\pi\alpha^2 \sqrt{(1+\frac{2}{\chi}+\frac{2}{\chi^2})} \frac{1}{\sqrt{1-\frac{2}{\chi}}} - \frac{5}{4} - \sin^2\beta(2\sin^2\beta-1) + \frac{4\cos^2\beta}{2(1+4)} + \frac{4\cos^2\beta}{2(1+4)}$



At the threshold $\sigma = \frac{dC}{\sqrt{2}} \frac{\sqrt{sin^2 \beta}}{\sin^2 \beta} \approx 2.2 \times 10^{-35} \frac{\sqrt{sin^2 \beta}}{\sin^2 \beta}$ (10)

In the most interesting region $s \ll m^4/m_o^2 (y \ll 1)$

$$\sigma = \frac{4\pi \lambda^2 V}{S} \left[\left(1 + \frac{2}{X} + \frac{2}{X^2} \right) \frac{L}{V} - \frac{5}{4} \right] \tag{11}$$

At 1m/s/m²/>>1m/m²/m²/)

$$\sigma = \frac{2\pi \alpha^2 (1 + 2\sin^4 \beta)}{S} \ln \frac{s}{m^2}$$
 (12)

The terms proportional to the masses of electron and X that are not presented here do not change the asymptotic behaviour of the cross-section.

We became aware that the reaction e'e W'W was considered also by A.E.Asratyan and M.A.Kuban-tsev.

3. Reaction ete -- ete W'W

Since the cross-section of the process e'eW'W decreases with energy, it is interesting to
consider the reaction e'e-e'e W'W which is of higher order in \(\pi \), but has the cross-section logarithmically increasing with energy.

For the following calculations we need the cross-section of the process 85-W*W (fig.5). Di-

Fig.5.

rect calculation of this cross-section gives

$$\overline{O_{XS}}(S) = \frac{2\pi d^2}{m^2} \mathcal{V} \left\{ 4 + \frac{3}{X} + \frac{12}{X^2} - \frac{12}{X^2} \left(1 - \frac{2}{X} \right) \frac{1}{V} \ln \frac{1 + V}{1 - V} \right\}$$
(13)

Here $x = s/m^2$, m is the W-boson mass, $v = \sqrt{1 - 4/x}$ is its c.m.s. velocity. This expression agrees with the corresponding formulae obtained in the paper/7/.

Note an interesting peculiarity of the process 88-W'W. As can be seen from the formula (13), The asymptotically tends to a constant. This behaviour differs drastically from that of cross-section of two-photon production of scalar and spinor particles, those decreasing like s and s ln(s) correspondingly. This asymptotics of of can be easily understood if one notes that at m-0 the reaction 88--W'W reduces to elastic scattering of vector particles in fact (one can verify easily that the presence of charge exchange does not influence the structure of matrix element). Since the exchange of vector particle contributes to this cross-section, at m = 0 the usual Coulomb divergence arises at small scattering angles. Non-zero mass of the exchange quantum makes the cross-section finite and not decreasing with energy. The cross-section is constant for W-boson helicities 1. For zero-helicity Wboson the cross-section decreases with energy like the production cross-section of scalar or spinor particles, due to change of helicity of real particles in vertices of exchange graphs.

Note that the specific feature of renormalizable theory, due to which the cross-section does not increase with energy, is that in this theory the g-factor of W-boson is equal to 2 (see also/7/).

We shall make all the following calculations restricting to the region s>>m², ln(s/m_e²)*ln(s/m²).

Knowing of, it is easy to compute the cross-section of the process &e-eWW. Non-decreasing with energy contribution to the cross-section is given only by the diagram 6. Using the covariant Weizsae-

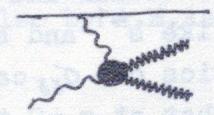


Fig.6.

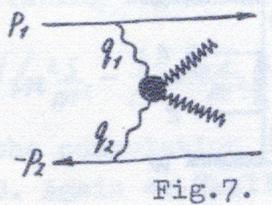
cker-Williams method/8/ and the expression (13) for we obtain

$$\sigma(8e-eww) = \frac{8d^3}{m^2} ln \frac{S}{m_e} [ln \frac{S}{m^2} - \frac{8}{3}]$$
 (14)

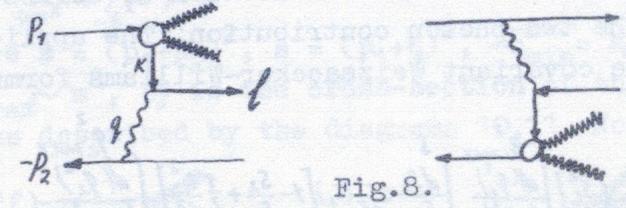
The cross-section of this process for nonrenormalizable electromagnetic interaction of W-bosons (which was found to be increasing linearly with energy) was calculated in the work/9/.

Return to the process ee-eeWW. The major contribution to its cross-section is given first of all

by the diagram 7. Two photon poles at this graph



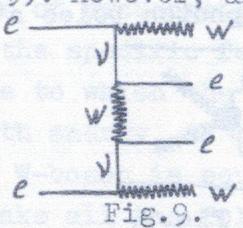
amplify its contribution $\sim \ln^2(s/m_e^2)$. It is necessary also generally speaking to take into account the diagrams 8, also doubly logarithmically amplified



by photon and fermion poles. These three diagrams do not interfere with the taken accuracy. Indeed, in the c.m.s. of initial particles under the two-photon mechanism the electron and positron almost do not change their directions of motion. At the same time, due to the presence of the fermion pole near the physical domain at the diagrams 8, the final etemion of the particle which emits the exchange formatum.

Besides the diagrams 7,8, there are some graphs whose contributions do not decrease with energy (e.g.,

that at the fig.9). However, all of them contain



lower degrees of ln(s/m_e) and therefore can be neglected with taken accuracy.

Compute at first the cross-section of corresponding to the two-photon contribution. The application of the covariant Weizsaecker-Williams formula gives

$$\sigma_{i} = \frac{d^{2}}{\sqrt{3}} \left\{ \frac{dS_{1}}{S_{1}} \left[1 - \frac{S_{1}}{S_{1}} + \frac{1}{2} \frac{S_{1}^{2}}{S_{2}^{2}} \right] \frac{d(Q_{1}^{2})}{(-Q_{1}^{2})} \right\} \left\{ \frac{dS_{2}}{S_{2}} \sigma_{i} \left(S_{2} \right) \left[1 - \frac{S_{2}}{S_{1}} + \frac{1}{2} \frac{S_{2}^{2}}{S_{1}^{2}} \right] \frac{d(Q_{2}^{2})}{(-Q_{2}^{2})} \right\} \left\{ \frac{d(Q_{2}^{2})}{(-Q_{1}^{2})} \right\} \left\{ \frac{d(Q_{2}^{2})}{S_{2}} \left(S_{2} \right) \left[1 - \frac{S_{2}}{S_{1}} + \frac{1}{2} \frac{S_{2}^{2}}{S_{1}^{2}} \right] \right\} \left\{ \frac{d(Q_{2}^{2})}{(-Q_{2}^{2})} \right\} \left\{ \frac{d(Q_{2}^{2})}{(-Q_{2}^{2})} \right\} \left\{ \frac{d(Q_{2}^{2})}{S_{2}} \right\} \left\{$$

(the notations of momenta see at the diagram 7), $-q_{1}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{1} \right), \quad -q_{1}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left(s_{1} - s_{2} \right), \quad -q_{2}^{2} = \frac{2^{2}}{3} \left($

$$\sigma_{1} = \frac{d^{2}}{\pi^{2}} \ln \frac{2S}{m_{e}^{2}} \int \frac{dS_{2}}{S_{2}} \sigma_{8\delta}(S_{2}) \left[\left(1 + \frac{1}{2} \frac{S_{2}}{S} \right)^{2} \ln \frac{S}{S_{2}} - \frac{3}{2} + \frac{S_{2}}{S} + \frac{1}{2} \frac{S_{2}^{2}}{S^{2}} \right]$$
(16)

Substituting the expression (13) for Orginto (16)

and integrating over s2, we obtain (holding only terms non-decreasing with energy)

$$\sigma_{1} = \frac{4d^{4}}{4m^{2}} \ln \frac{1}{m^{2}} \left[\ln \frac{2S}{m^{2}} - \frac{41}{6} \ln \frac{S}{m^{2}} + \frac{215}{12} - \frac{71^{2}}{3} \right]$$
 (17)

Pass to the computation of σ_2 corresponding to the diagrams 8. Again we shall use the covariant formulation of the Weizsaecker-Williams method:

$$\sigma_{2} = \frac{d}{dt} \int \frac{dS_{8}}{S_{8}} \int \frac{d(t-q^{2})}{(t-q^{2})} \left[1 - \frac{S_{8}}{S} + \frac{1}{2} \frac{S_{8}^{2}}{S^{2}}\right] \sigma_{8}(S_{8}, q^{2})$$
(18)

Here $s = (p_1+p_2)^2$, $s = (p_1+q)^2$, $-q_{\min}^2 = s_e^2 m_e^2/s(s-s_e)$, $-q_{\max}^2 m^2$, σ_e is the cross-section of the photoprocess described by the diagrams 10,11. Note that in

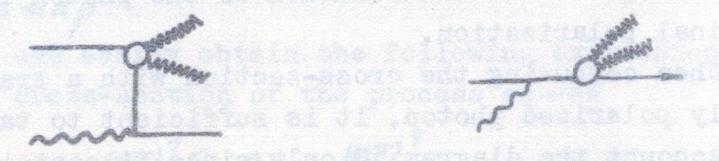


Fig. 10.

Fig.11.

the formula (18) it is necessary to take into account the dependence of the σ_{ℓ} on the photon mass q^2 . This circumstance is connected with the nearness of the fermion pole to the physical domain.

For the computation of the photoprocess crosssection the covariant summation over photon polarizations is inconvenient since it should be carried out with gauge-invariant block, i.e., it requires taking into account both diagrams 10,11.

Under uncovariant summation it is necessary, generally speaking, to take into account the longitudinal polarization of 8-quantum. This polarization or vector is as follows:

$$\xi_{M} = \frac{1}{\sqrt{9^{2}}}g_{M} + \frac{\sqrt{9^{2}}}{g_{o}+|\vec{q}|}(-1, |\vec{q}|)$$

The first term does not contribute, due to gauge invariance. The second term is proportional to the photon mass $\sqrt{q^2}$ and therefore after integration over q^2 in the formula (18) it will not lead to logarithmic amplification. Thus with taken accuracy one can neglect the contribution of the photon longitudinal polarization.

When computing the cross-section with a transversely polarized photon, it is sufficient to take into account the diagram 10 only since it contains a fermion pole near the physical domain and is therefore logarithmically amplified by itself. Square of the amplitude corresponding to the diagram 10 averaged over polarizations of initial electron and summed over polarizations of final one, after integration over W-boson momenta looks as follows

$$M^2 \sim Sp\{\{\hat{\epsilon} \frac{\hat{k}}{K^2 - m_e^2} \hat{\rho}(P, K) \frac{\hat{k}}{K^2 - m_e^2} \hat{\epsilon}\}$$
 (19)

Here ℓ_n is the three-dimensionally transverse polarization of the photon, $\hat{\rho}(p,k)$ is a matrix that describes the interaction in the upper block (the momenta notations are given at the diagram 10). General representation of the matrix $\hat{\rho}$ is the following:

$$\hat{\rho} = a\hat{\rho} + \theta\hat{R} \tag{20}$$

(It can be verified easily that other combinations of %-matrices drop out when the trace is taken). In the formula (19) it is necessary to hold only the terms with a pole in k². This circumstance allows one to neglect the second term in the formula (20), i.e.,

$$\hat{p} = a\hat{p} \tag{21}$$

One can easily obtain the following expression for the cross-section of the process ee--WW

$$\sigma_{ee}(s_i) = \frac{(271)^4}{8s_i} S_p \hat{\rho} \hat{R} = \frac{(271)^4}{4} a. \tag{22}$$

Using the formulae (20)-(22) and carrying out the summation over photon transverse polarizations, we obtain

$$G_8 = \frac{d}{2\pi S_8} \int_{S_7}^{S_8} \int_{m_e^2 - K^2}^{K_{max}} G_{ee}(S_7) \left[1 - 2\frac{S_1}{5} + 2\frac{S_1^2}{5^2} \right]$$

$$4m^2 - K_{min}$$
(25)

where
$$-k_{\min}^2 \sim -q^2 s_1/s$$
, $-k_{\max}^2 \sim m^2$.

Note that the way of calculation of the pole

contribution to the cross-section presented above, is in fact the covariant formulation of the so-called method of quasireal electrons given in the works/10, 11/.

The substitution of the expression (23) into the formula (18) and integration over k^2 , q^2 and S_7 with logarithmic accuracy give

$$\sigma_{2} = \frac{d^{2}}{4\pi^{2}} \left(n \frac{2}{m^{2}} \frac{S^{2}}{m^{2}} \int_{4m^{2}}^{S} \frac{dS_{1}}{S_{1}} \left[\frac{2}{3} + \frac{1}{2} \frac{S_{1}}{3} - \frac{1}{2} \frac{S_{1}^{2}}{3} - \frac{2}{3} \frac{S_{3}^{3}}{5^{3}} - \frac{S_{1}}{5} (1 + \frac{S_{1}}{5}) \ln \frac{S}{S_{1}} \right] \sigma_{ee}(S_{1})(24)$$

Computation of the integral over s_1 (accounting for the terms non-decreasing with energy only) leads to the following expressions for the cross-section: in the Georgi-Glashow model (at $m^2 \ll s \ll m^4/m_o^2$)

$$\sigma_{2} = \frac{139}{540 \, \text{Ti} \, m^{2}} \, \ln^{2} \frac{5}{m_{s}^{2}} \tag{25}$$

in the Weinberg model

$$\sqrt{2} = \frac{d^4}{32\pi m^2 sin^4 \eta} \xi \ln \frac{25}{m_e^2}$$
(26)

where $\xi = 1.1$; 1.15; 1.25 at $\sin^2 \eta = 0.2$; 0.3; 0.4 correspondingly.

The total cross-section of the process ee-eeWW is evidently equal to

$$abla = \sigma_1 + 2\sigma_2 \tag{27}$$

In this formula the second term is by one or two or-

ders of magnitude smaller than the first one, i.e., the contribution of the diagram 5 is small numerically. From the comparison of the formula (6) or (11) with (17) it can be seen that the process eeeewW dominates over eeeWW already at the energy $2E = \sqrt{s} \approx 14m$. In this region the cross-section found by means of the formula (17) differs from the result of the numerical computations using the formula (16) not more than by some per cent.

The cross-section of the process ee-eeWW was computed in the work/12/. The result for the contribution of the diagram 4 differs considerably from ours. We cannot point out the cause of this discrepancy since the computation of The in the mentione work was made by numerical methods. Besides, in the work/12/ the contribution of the diagram 8 was not considered.

The authors are grateful to A.N.Skrinsky and A.I.Vainshtein for valuable discussions.

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